Please check the examination details belo	w before ente	ering your candidate information
Candidate surname		Other names
Centre Number Candidate Nu Pearson Edexcel Level		
Friday 19 May 2023		
Afternoon	Paper reference	8FM0/24
Further Mathema Advanced Subsidiary Further Mathematics option 24: Further Statistics 2 (Par	ons	tion G only)
You must have: Mathematical Formulae and Statistical	Tables (Gre	een), calculator

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 - there may be more space than you need.
- You should show sufficient working to make your methods clear.
 Answers without working may not gain full credit.
- Values from statistical tables should be quoted in full. If a calculator is used instead of tables the value should be given to an equivalent degree of accuracy.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- The total mark for this part of the examination is 40. There are 4 questions.
- The marks for each question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over







1. Every applicant for a job at *Donala* is given three different tasks, *P*, *Q* and *R*. For each task the applicant is awarded a score.

The scores awarded to 9 of the applicants, for the tasks P and Q, are given below.

Applicant	A	В	С	D	E	F	G	Н	I
Task P	19	16	16	12	8	17	12	12	5
Task Q	17	11	14	7	6	18	15	11	10

(a) Calculate Spearman's rank correlation coefficient for the scores awarded for the tasks P and Q.

(4)

(b) Test, at the 1% level of significance, whether or not there is evidence for a positive correlation between the ranks of scores for tasks *P* and *Q*. You should state your hypotheses and critical value clearly.

(4)

The Spearman's rank correlation coefficient for P and R is 0.290 and for Q and R is 0.795

The manager of *Donala* wishes to reduce the number of tasks given to job applicants from three to two.

(c) Giving a reason for your answer, state which 2 tasks you would recommend the manager uses.

(2)



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Question 1 continued	
(То	tal for Question 1 is 10 marks)



2. A continuous random variable X has probability density function

$$f(x) = \begin{cases} \frac{x}{16}(9 - x^2) & 1 \le x \le 3\\ 0 & \text{otherwise} \end{cases}$$

(a) Find the cumulative distribution function of X

(3)

(b) Calculate P(X > 1.8)

(2)

(c) Use calculus to find $E\left(\frac{3}{X} + 2\right)$

(3)

(d) Show that the mode of *X* is $\sqrt{3}$

(3)



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Question 2 continued



Question 2 continued

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Question 2 continued	
	(Total for Question 2 is 11 marks)



3. Pat is investigating the relationship between the height of professional tennis players and the speed of their serve. Data from 9 randomly selected professional male tennis players were collected. The variables recorded were the height of each player, h metres, and the maximum speed of their serve, v km/h.

Pat summarised these data as follows

$$\sum h = 17.63$$

$$\sum v = 2174.9$$

$$\sum h = 17.63$$
 $\sum v = 2174.9$ $\sum v^2 = 526407.8$ $S_{hh} = 0.0487$ $S_{hv} = 5.1376$

$$S_{hh} = 0.0487$$

$$S_{hv} = 5.1376$$

(a) Calculate the product moment correlation coefficient between h and v

(2)

(b) Explain whether the answer to part (a) is consistent with a linear model for these data.

(1)

(c) Find the equation of the regression line of v on h in the form v = a + bhwhere a and b are to be given to one decimal place.

(3)

Pat calculated the sum of the residuals for the 9 tennis players as 1.04

(d) Without doing a calculation, explain how you know Pat has made a mistake.

(1)

Pat made one mistake in the calculation. For the tennis player of height 1.96 m Pat misread the residual as 2.27

(e) Find the maximum speed of serve, in km/h, for the tennis player of height 1.96 m

(3)

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Question 3 continued	
	(Total for Organian 2 !- 10
	(Total for Question 3 is 10 marks)



- **4.** The random variable *X* has a continuous uniform distribution over the interval [-3, k] Given that $P(-4 < X < 2) = \frac{1}{3}$
 - (a) find the value of k

(3)

A computer generates a random number, Y, where

- Y has a continuous uniform distribution over the interval [a, b]
- E(Y) = 6
- Var(Y) = 192

The computer generates 5 random numbers.

(b) Calculate the probability that at least 2 of the 5 numbers generated are greater than 7.5

(6)

Question 4 continued



Question 4 continued	
	(Total for Question 4 is 9 marks)
,	TOTAL FOR FURTHER STATISTICS 2 IS 40 MARKS

